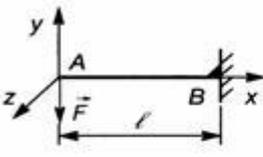
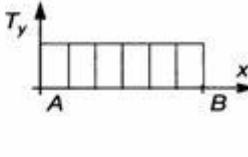
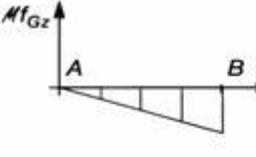
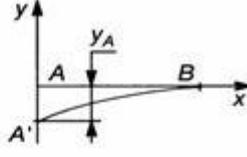
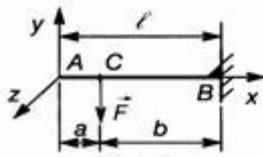
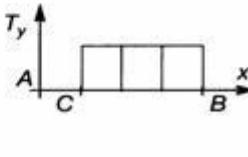
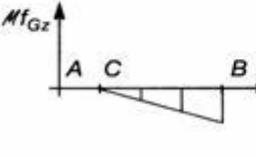
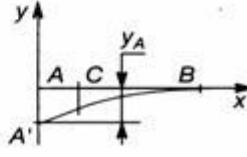
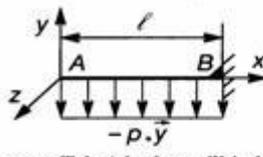
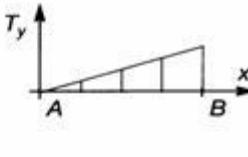
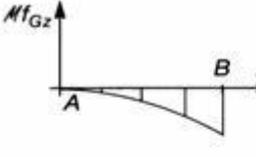
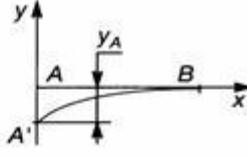
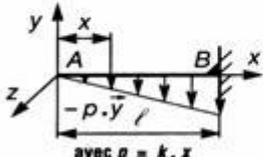
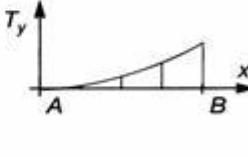
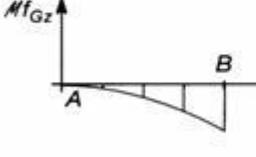
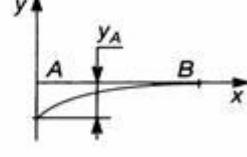
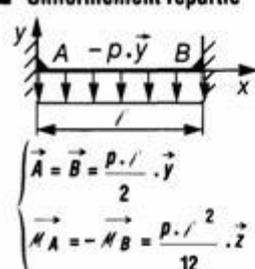
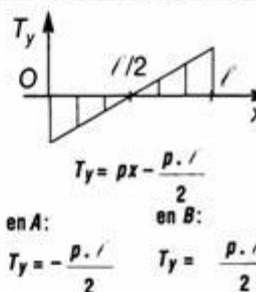
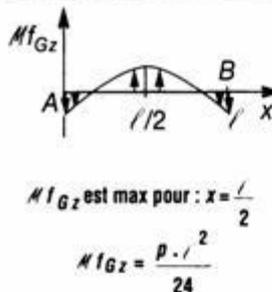
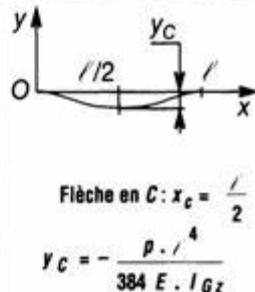
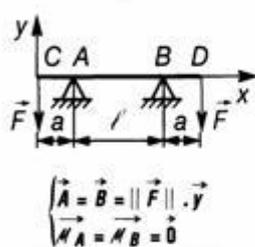
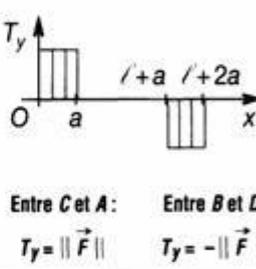
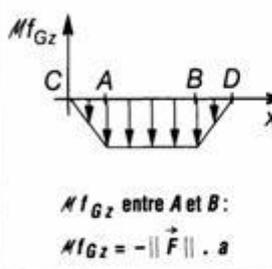
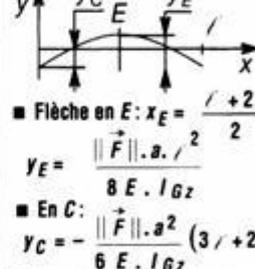
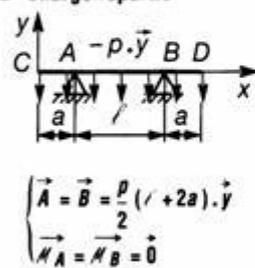
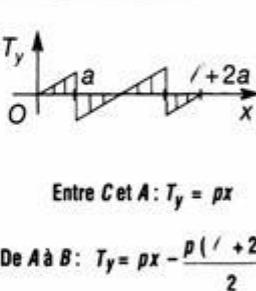
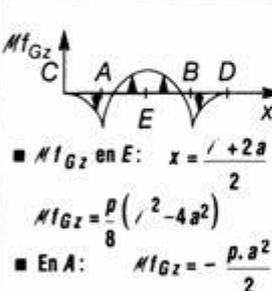
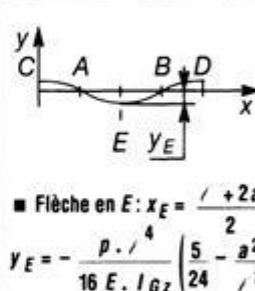
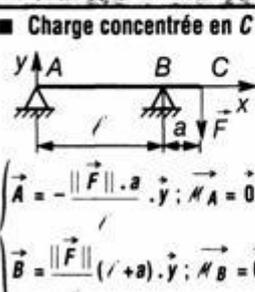
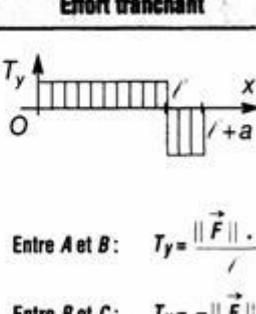
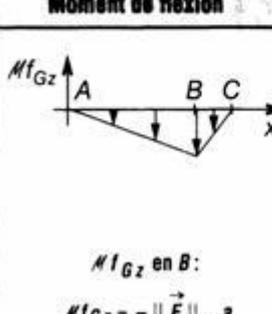
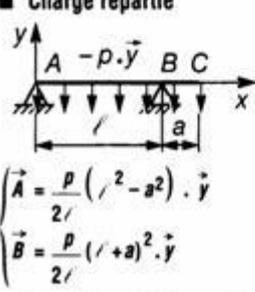
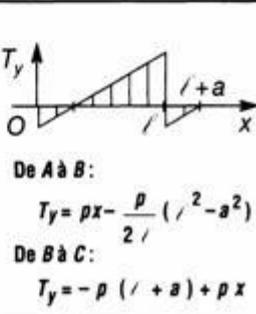
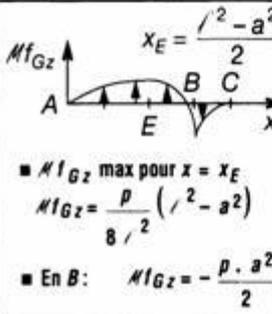
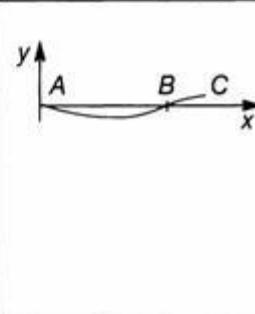
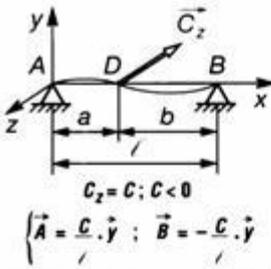
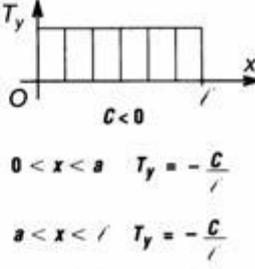
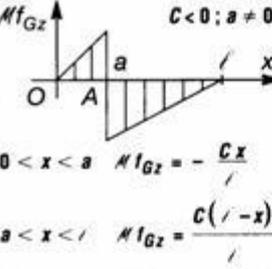
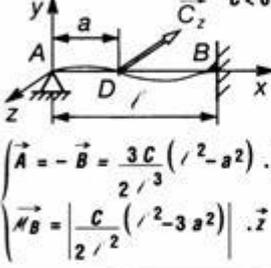
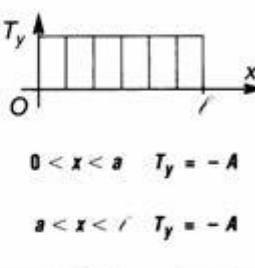
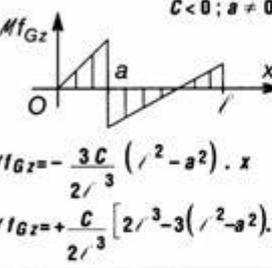
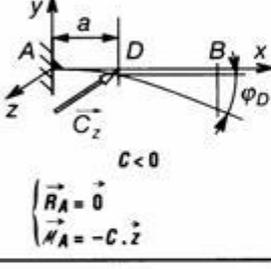
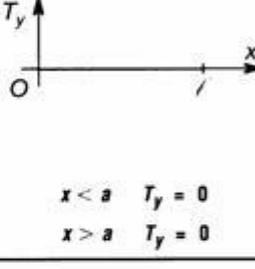
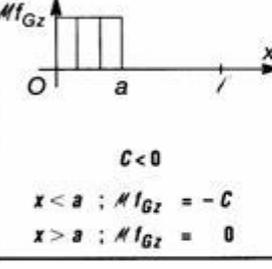
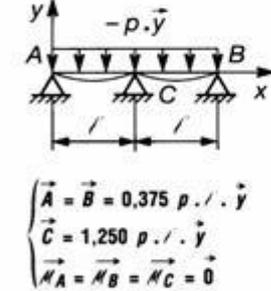
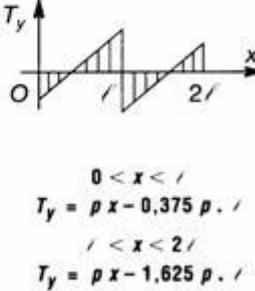
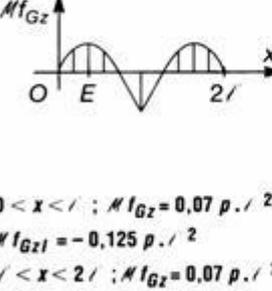
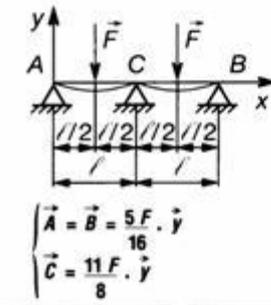
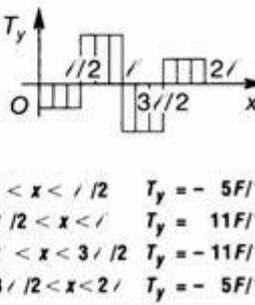
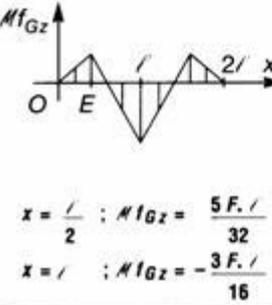


La Flexion :

POUTRES SUR UN APPUI			
Charges - Appuis	Effort tranchant	Moment de flexion	Déformation
<p>■ Concentrée en A</p>  $\begin{cases} \vec{B} = -\vec{F} = \ \vec{F}\ \cdot \vec{y} \\ \text{(avec } F < 0) \\ \vec{M}_B = -\ \vec{F}\ \cdot l \cdot \vec{z} \end{cases}$	 <p style="text-align: center;">avec $F < 0$</p> <p style="text-align: center;">$T_y = +\ \vec{F}\$</p> <p style="text-align: center;">constant entre A et B</p>	 <p style="text-align: center;">avec $F < 0$</p> <p style="text-align: center;">Moment de flexion</p> <p style="text-align: center;">en B : $M_{Gz} = -\ \vec{F}\ \cdot l$</p>	 <p style="text-align: center;">Flèche en A : $F < 0$</p> <p style="text-align: center;">$y_A = -\frac{\ \vec{F}\ \cdot l^3}{3E \cdot I_{Gz}}$</p>
<p>■ Concentrée en C</p>  $\begin{cases} \vec{B} = -\vec{F} \\ \text{avec } F < 0 \\ \vec{B} = \ \vec{F}\ \cdot \vec{y} \\ \vec{M}_B = -\ \vec{F}\ \cdot b \cdot \vec{z} \end{cases}$	 <p style="text-align: center;">Entre A et C : $T_y = 0$</p> <p style="text-align: center;">Entre C et B : avec $F < 0$</p> <p style="text-align: center;">$T_y = \ \vec{F}\$</p>	 <p style="text-align: center;">Moment de flexion en B : avec $F < 0$</p> <p style="text-align: center;">$M_{Gz} = -\ \vec{F}\ \cdot b$</p>	 <p style="text-align: center;">Flèche en A :</p> <p style="text-align: center;">$y_A = -\frac{\ \vec{F}\ \cdot (l-a)^2 (2l+a)}{6E \cdot I_{Gz}}$</p>
<p>■ Uniformément répartie</p>  <p>p : coefficient de charge (N/m)</p> $\begin{cases} \vec{B} = p \cdot l \cdot \vec{y} \\ \vec{M}_B = -\frac{p \cdot l^2}{2} \cdot \vec{z} \end{cases}$	 <p style="text-align: center;">Effort tranchant max en B :</p> <p style="text-align: center;">$T_{y \max} = p \cdot l$</p>	 <p style="text-align: center;">Moment de flexion en B :</p> <p style="text-align: center;">$M_{Gz} = -\frac{p \cdot l^2}{2}$</p>	 <p style="text-align: center;">Flèche en A :</p> <p style="text-align: center;">$y_A = -\frac{p \cdot l^4}{8E \cdot I_{Gz}}$</p>
<p>■ Linéairement répartie</p>  <p>avec $p = k \cdot x$</p> $\begin{cases} \vec{B} = \frac{k \cdot l^2}{2} \cdot \vec{y} \\ \vec{M}_B = -\frac{k \cdot l^3}{6} \cdot \vec{z} \end{cases}$	 <p style="text-align: center;">Effort tranchant max en B :</p> <p style="text-align: center;">$T_{y \max} = \frac{k \cdot l^2}{2}$</p>	 <p style="text-align: center;">Moment de flexion en B :</p> <p style="text-align: center;">$M_{Gz} = -\frac{k \cdot l^3}{6}$</p>	 <p style="text-align: center;">Flèche en A :</p> <p style="text-align: center;">$y_A = -\frac{k \cdot l^5}{30E \cdot I_{Gz}}$</p>

Charges - Appuis	Effort tranchant	Moment de flexion	Déformation
<p>■ Uniformément répartie</p>  $\begin{cases} \vec{A} = \vec{B} = \frac{p \cdot l}{2} \cdot \vec{y} \\ \vec{M}_A = -\vec{M}_B = \frac{p \cdot l^2}{12} \cdot \vec{z} \end{cases}$	 $T_y = px - \frac{p \cdot l}{2}$ <p>en A: $T_y = -\frac{p \cdot l}{2}$ en B: $T_y = \frac{p \cdot l}{2}$</p>	 $Mf_{Gz} \text{ est max pour : } x = \frac{l}{2}$ $Mf_{Gz} = \frac{p \cdot l^2}{24}$	 <p>Flèche en C: $x_C = \frac{l}{2}$</p> $y_C = -\frac{p \cdot l^4}{384 E \cdot I_{Gz}}$
POUTRE SUR DEUX APPUIS AVEC PORTE-À-FAUX SYMÉTRIQUE			
Charges - Appuis	Effort tranchant	Moment de flexion	Déformation
<p>■ Deux charges concentrées</p>  $\begin{cases} \vec{A} = \vec{B} = \ \vec{F}\ \cdot \vec{y} \\ \vec{M}_A = \vec{M}_B = \vec{0} \end{cases}$	 <p>Entre C et A: $T_y = \ \vec{F}\$ Entre B et D: $T_y = -\ \vec{F}\$</p>	 <p>Mf_{Gz} entre A et B: $Mf_{Gz} = -\ \vec{F}\ \cdot a$</p>	 <p>Flèche en E: $x_E = \frac{l + 2a}{2}$</p> $y_E = \frac{\ \vec{F}\ \cdot a \cdot l^2}{8 E \cdot I_{Gz}}$ <p>En C: $y_C = -\frac{\ \vec{F}\ \cdot a^2}{6 E \cdot I_{Gz}} (3l + 2a)$</p>
<p>■ Charge répartie</p>  $\begin{cases} \vec{A} = \vec{B} = \frac{p}{2} (l + 2a) \cdot \vec{y} \\ \vec{M}_A = \vec{M}_B = \vec{0} \end{cases}$	 <p>Entre C et A: $T_y = px$</p> <p>De A à B: $T_y = px - \frac{p(l + 2a)}{2}$</p>	 <p>Mf_{Gz} en E: $x = \frac{l + 2a}{2}$</p> $Mf_{Gz} = \frac{p}{8} (l^2 - 4a^2)$ <p>En A: $Mf_{Gz} = -\frac{p \cdot a^2}{2}$</p>	 <p>Flèche en E: $x_E = \frac{l + 2a}{2}$</p> $y_E = -\frac{p \cdot l^4}{16 E \cdot I_{Gz}} \left(\frac{5}{24} - \frac{a^2}{l^2} \right)$
POUTRES SUR DEUX APPUIS AVEC PORTE-À-FAUX UNILATÉRAL			
Charges - Appuis	Effort tranchant	Moment de flexion	Déformation
<p>■ Charge concentrée en C</p>  $\begin{cases} \vec{A} = -\frac{\ \vec{F}\ \cdot a}{l} \cdot \vec{y}; \vec{M}_A = \vec{0} \\ \vec{B} = \frac{\ \vec{F}\ (l + a)}{l} \cdot \vec{y}; \vec{M}_B = \vec{0} \end{cases}$	 <p>Entre A et B: $T_y = \frac{\ \vec{F}\ \cdot a}{l}$</p> <p>Entre B et C: $T_y = -\ \vec{F}\$</p>	 <p>Mf_{Gz} en B: $Mf_{Gz} = -\ \vec{F}\ \cdot a$</p>	 <p>Flèche en E: $x = \frac{l \sqrt{3}}{3}$</p> $y_E = \frac{\ \vec{F}\ \cdot a \cdot l^2 \sqrt{3}}{27 E \cdot I_{Gz}}$ <p>en C: $y_C = -\frac{\ \vec{F}\ \cdot a^2 (a + l)}{3 E \cdot I_{Gz}}$</p>
<p>■ Charge répartie</p>  $\begin{cases} \vec{A} = \frac{p}{2l} (l^2 - a^2) \cdot \vec{y} \\ \vec{B} = \frac{p}{2l} (l + a)^2 \cdot \vec{y} \end{cases}$	 <p>De A à B: $T_y = px - \frac{p}{2l} (l^2 - a^2)$</p> <p>De B à C: $T_y = -p(l + a) + px$</p>	 <p>Mf_{Gz} max pour $x = x_E$</p> $Mf_{Gz} = \frac{p}{8l^2} (l^2 - a^2)$ <p>En B: $Mf_{Gz} = -\frac{p \cdot a^2}{2}$</p>	

POUTRES SUPPORTANT UN COUPLE			
Charges - Déformées	Effort tranchant	Moment de flexion	Déformation
 <p> $C_2 = C; C < 0$ $\vec{A} = \frac{C}{l} \cdot \vec{y}; \vec{B} = -\frac{C}{l} \cdot \vec{y}$ </p>	 <p> $0 < x < a \quad T_y = -\frac{C}{l}$ $a < x < l \quad T_y = -\frac{C}{l}$ </p>	 <p> $C < 0; a \neq 0$ $0 < x < a \quad Mf_{Gz} = -\frac{Cx}{l}$ $a < x < l \quad Mf_{Gz} = \frac{C(l-x)}{l}$ </p>	<p>Flèche en D:</p> $y_D = \frac{1}{E \cdot I_{Gz}} \cdot \frac{C \cdot a \cdot b (b-a)}{3}$ $\varphi_A = -\frac{C}{6E \cdot I_{Gz} \cdot l} \cdot (l^2 - 3b^2)$ $\varphi_B = -\frac{C}{6E \cdot I_{Gz} \cdot l} \cdot (l^2 - 3a^2)$
 <p> $C < 0$ $\vec{A} = -\vec{B} = \frac{3C}{2l^3} (l^2 - a^2) \cdot \vec{y}$ $\vec{M}_B = \left \frac{C}{2l^2} (l^2 - 3a^2) \right \cdot \vec{z}$ </p>	 <p> $0 < x < a \quad T_y = -A$ $a < x < l \quad T_y = -A$ </p>	 <p> $C < 0; a \neq 0$ $Mf_{Gz} = -\frac{3C}{2l^3} (l^2 - a^2) \cdot x$ $Mf_{Gz} = +\frac{C}{2l^3} [2l^3 - 3(l^2 - a^2) \cdot x]$ </p>	<p> $0 < x < a$ $y = -\frac{C(l-a)x}{4E \cdot I_{Gz} \cdot l^3} \dots$ $\dots [l^2(3a-l) - (l+a)x^2]$ </p> $\varphi_A = -\frac{C}{4E \cdot I_{Gz} \cdot l} (l-a)(l-3a)$
 <p> $C < 0$ $\vec{R}_A = \vec{0}$ $\vec{M}_A = -C \cdot \vec{z}$ </p>	 <p> $x < a \quad T_y = 0$ $x > a \quad T_y = 0$ </p>	 <p> $C < 0$ $x < a; Mf_{Gz} = -C$ $x > a; Mf_{Gz} = 0$ </p>	$f_D = \frac{C \cdot a^2}{2E \cdot I_{Gz}}$ $f_B = \frac{C \cdot a}{E \cdot I_{Gz}} \left(\frac{l-a}{2} \right)$ $\varphi_D = \frac{C \cdot a}{E \cdot I_{Gz}} = \varphi_B$
POUTRES SUR TROIS APPUIS DE NIVEAU			
 <p> $\vec{A} = \vec{B} = 0,375 p \cdot l \cdot \vec{y}$ $\vec{C} = 1,250 p \cdot l \cdot \vec{y}$ $\vec{M}_A = \vec{M}_B = \vec{M}_C = \vec{0}$ </p>	 <p> $0 < x < l$ $T_y = px - 0,375 p \cdot l$ $l < x < 2l$ $T_y = px - 1,625 p \cdot l$ </p>	 <p> $0 < x < l; Mf_{Gz} = 0,07 p \cdot l^2$ $Mf_{Gz} = -0,125 p \cdot l^2$ $l < x < 2l; Mf_{Gz} = 0,07 p \cdot l^2$ </p>	<p>Flèche pour $x_E = 0,42 l$</p> $f_E = -0,043 \frac{p \cdot l^4}{E \cdot I_{Gz}}$
 <p> $\vec{A} = \vec{B} = \frac{5F}{16} \cdot \vec{y}$ $\vec{C} = \frac{11F}{8} \cdot \vec{y}$ </p>	 <p> $0 < x < l/2 \quad T_y = -5F/16$ $l/2 < x < l \quad T_y = 11F/16$ $l < x < 3/2 \quad T_y = -11F/16$ $3/2 < x < 2 \quad T_y = -5F/16$ </p>	 <p> $x = \frac{l}{2}; Mf_{Gz} = \frac{5F \cdot l}{32}$ $x = l; Mf_{Gz} = -\frac{3F \cdot l}{16}$ </p>	<p>pour $x_E = \frac{l \sqrt{5}}{5}$</p> $f_E = -\frac{F \cdot l^3}{240 E \cdot I_{Gz}}$